

PreCalculus Trimester B

Name Key Hr \_\_\_\_\_

Final Review Part 1

Determine whether the following are polynomial functions and if they are, state the degree.

1.  $14x^2 + 2x^{1/3} - 5$  no, because of  $1/3$  exponent.

2.  $(x-3)^2(x+7)$  yes, degree 3.

Find all the real zeros and state their multiplicities.

3.  $2(x-7)^4(x+3)^2$   
7 mult. 4, -3 mult. 2

4.  $x^2 + 5x - 50$   
 $(x+10)(x-5)$   
-10 mult 1, 5 mult. 1

Find a polynomial of minimum degree that has the given zeros.

5. 3, 7, -2  $(x-3)(x-7)(x+2)$

6. -5 (multiplicity 2), 4 (multiplicity 3)

$(x+5)^2(x-4)^3$

For the following polynomial (a) list each real zero and its multiplicity (b) determine whether the graph touches or crosses at each x-intercept (c) find the y-intercept (d) sketch the graph.

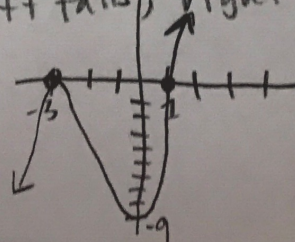
7.  $f(x) = (x-1)(x+3)^2$

c)  $f(0) = (0-1)(0+3)^2 = (-1)(9) = -9$

a) 1 mult 1  
-3 mult. 2

d) degree is 3 & function is positive so left falls, right rises.

b) crosses at 1 (since mult. is odd)  
touches at -3 (since mult. is even)

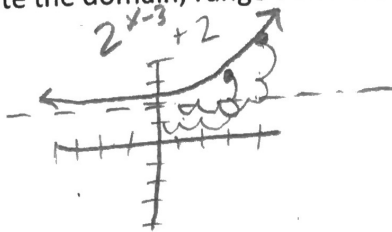
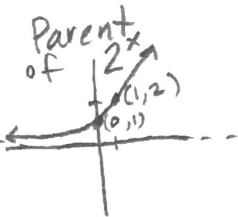




8. Evaluate  $30e^{t(3.2)}$  when  $t = 15$ .

$$30e^{(15)(3.2)} = 2.105 \times 10^{22}$$

9. State the domain, range and horizontal asymptote of:  $f(x) = 2^{x-3} + 2$  up 2



domain:  $(-\infty, \infty)$   
 range:  $(2, \infty)$   
 h.a.:  $y = 2$

10. \$1550 dollars is invested in an account that pays 7% interest compounded continuously.

What will the balance in the account be after 12 years? ( $A = Pe^{rt}$ )

$A = ?$   $r = 0.07$   
 $P = 1550$   $t = 12$

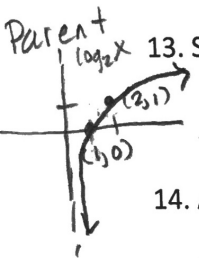
$$A = 1550e^{(0.07)(12)} = \$3590.37$$

11. Write in exponential form:  $\log_2 16 = 4$

$$2^4 = 16$$

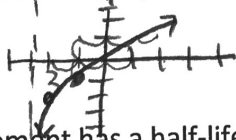
12. Write in logarithmic form:  $4^3 = 64$

$$\log_4 64 = 3$$



13. State the domain and vertical asymptote of:  $f(x) = \log_2(x+3) - 2$  left 3 down 2

$\log_2(x+3) - 2$



domain:  $(-3, \infty)$   
 v.a.:  $x = -3$

14. A certain radioactive element has a half-life of 840 years. There are 20 pounds of this

substance initially. How much will there be after 1700 years? ( $y = a(b)^{t/p}$ )

$$y = 20\left(\frac{1}{2}\right)^{\frac{1700}{840}} = 4.9 \text{ pounds}$$

$a = 20$  pounds  
 $b = \frac{1}{2}$   
 $p = 840$  yrs  
 $t = 1700$  yrs  
 $y = ?$

15. The number of bacteria in a culture doubles every 4 hours. There are 90 bacteria initially.

How long until there will be 459 bacteria?

$$459 = 90(2)^{t/4}$$

$$t = 4 \left( \frac{\log 5.1}{\log 2} \right) = 9.4 \text{ hours}$$

$b = 2$   
 $p = 4$  hrs  
 $a = 90$   
 $t = ?$   
 $y = 459$

$\frac{459}{90} = \frac{90(2)^{t/4}}{90}$   
 $5.1 = 2^{t/4}$   
 $\log_2 5.1 = t/4$   
 $t = 4 \log_2 5.1 =$